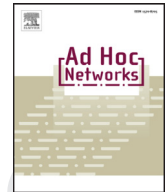




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Toward cluster-based weighted compressive data aggregation in wireless sensor networks

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ABSTRACT

Conventional Compressive Sampling (CS)-based data aggregation methods require a large number of sensor nodes for each CS measurement leading to an inefficient energy consumption in Wireless Sensor Networks (WSNs). To solve this problem, we propose a new scheme in the network layer, called “Weighted Compressive Data Aggregation (WCDA)”, which benefits from the advantage of the sparse random measurement matrix to reduce the energy consumption. The novelty of the WCDA algorithm lies in the power control ability in sensor nodes to form energy efficient routing trees with focus on the load-balancing issue. In the second part, we present another new data aggregation method namely “Cluster-based Weighted Compressive Data Aggregation (CWCDA)” to make a significant reduction in the energy consumption in our WSN model. The main idea behind this algorithm is to apply the WCDA algorithm to each cluster in order to reduce significantly the number of involved sensor nodes during each CS measurement. In this case, candidate nodes related to each collector node are selected among the nodes inside one cluster. This yields in the formation of collection trees with a smaller structure than that of the WCDA algorithm. The effectiveness of these new algorithms is evaluated from the energy consumption, load balancing and lifetime perspectives of the network. A comprehensive numerical evaluation is performed which shows that the performance of the proposed WCDA and CWCDA algorithms is significantly better than some existing data aggregation methods such as plain-CS, hybrid-CS and the Minimum Spanning Tree Projection (MSTP) schemes.

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1. Introduction

1.1. Background

Wireless Sensor Networks (WSNs) are commonly recognized as a new technology consisting of a large number of independent wireless sensor nodes with a spatial distribution to support a wide variety of applications, including

natural environment monitoring, medical services, surveillance and ocean pollution detection [1,2]. In a large-scale proactive WSN, each sensor node performs periodically some operations such as computing, sensing and self-organizing to transmit specific data to the sink node through multiple paths [3]. In such a configuration, sensors are typically powered by limited lifetime batteries, which are hard to be replaced or recharged. Other resource constraints in WSNs are short communication range, low bandwidth, limited processing/storage and in particular, the energy consumption. Energy consumption is mainly addressed in the following three stages: sensing, data processing, and data transmission. Generally, sensing and data processing have less energy consumptions than that of data transmission. Indeed,

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any reduction in the transmission cost can prolong the WSN's lifetime. Thus, minimizing the total energy consumption is of high importance in designing WSNs [4]. Numerous research works have addressed the energy efficiency challenge in WSNs from different perspectives, including energy conserving sleep scheduling [5], topology control [6], mobile data collectors [7], and data aggregation [8]. Central to this study is to deploy proper data aggregation and routing methods in a WSN to enhance both the energy consumption and the network's lifetime with taking the effect of load balancing into account.

With focus on the spatial correlation properties of sensed data in real WSNs, the number of data transmissions can be reduced by compression techniques to achieve a relatively high accuracy of recovery at the sink node. The spatial correlation of sensed data leads to an inherent sparsity of data in a proper basis such as Discrete Cosine Transform (DCT) domain or wavelet domain [9]. This means that a few number of data samples are nonzero or equivalently, a basis can be found in which the sensed data is sparse. To address the sparsity of such signals, Compressive Sensing (CS) theory [10,11] is employed as a newly emerged signal processing technique for efficiently compressing signals and accurately reconstructing of sparse and compressible signals. Unlike the Nyquist criterion, in CS theory, signals can be recovered using much fewer measurements than their original dimensions. More precisely, considering the inherent sparsity features and the spatial correlation of input signals in a correlated WSN, a CS-based data aggregation method forms a random measurement matrix via non-adaptive linear measurements to compress the corresponded data, and then reconstructs these signals through an optimization process [12].

1.2. Related work

In recent years, the attention of researchers has been devoted to utilizing CS-based data aggregation methods to increase the network's lifetime by reducing the amount of data transmissions and balancing the traffic load throughout the whole WSN (e.g. [13–17]). The first study on the decentralized CS-based data aggregation method in WSNs was framed in [13]. The technique in [13] simultaneously computes random measurements of the sensed data and broadcasts them throughout the network using a simple gossiping algorithm. This line of work was further expanded in [14] by incorporating an efficient Compressive Data Aggregation (CDA) method to improve both transmissions cost and the network's lifetime in large-scale WSNs. The authors in [14] analyze the network's capacity using the CDA method and prove that the capacity is proportional to the sparsity level of sensed data. In this method, the total data transmissions are decreased only when the number of required measured samples is small enough. Nevertheless, it is shown numerically in [14] that an increase in the number of measured samples leads to an increment in the number of network's transmissions when compared to the non-CS method. Reference [15] introduces an adaptive data aggregation method which applies CS on the local spatial correlation among data of neighboring sensor nodes. In [16], the authors propose a CS-based data aggregation scheme to reconstruct data at the sink node. The results show that the proposed data aggregation method

depends on the network's structure, while the compression matrix design is related to the sensed data. However, the scheme in [16] cannot automatically match the features of complex spatio-temporal correlation data. Reference [17] introduces a hybrid-CS data aggregation algorithm to achieve a high throughput in a WSN. The authors in [17] claim that since the measurement matrix is not sparse enough, applying a plain-CS may not yield a significant improvement in the throughput, while, it can result in a high throughput in the hybrid-CS method.

So far, the interaction between routing and CS-based data aggregation has been a barrier toward the progress in the field of energy consumption in WSNs [18,19]. These techniques utilize both routing and CS-based data aggregation methods to reduce the data traffic. In [18], the authors present a CS-based scheme which considers both routing and compression methods to minimize the energy consumption required for data collection in a WSN. However, this study does not consider the minimization of the energy consumption for transmission of each CS measurement. Most recent data aggregation methods which rely on dense random measurements have not highlighted this fact that a large number of elements in the random measurement matrix may be zero. Reference [20] addresses this issue and proposes a distributed sparse random measurement by which the significant information of a compressible signal can be reconstructed. The authors in [20] claim that each CS measurement only needs a combination of some sensed data instead of using all of them. In addition, it is shown in [20] that using the sparse random measurement considerably reduces the energy consumption of WSNs. However, the transmission cost in the gathering process of measured samples in multi-hop WSNs is not considered in this study. Routing and CS are also jointly addressed in [21] in which the routing path is iteratively built through a greedy choice to minimize the coherence measurements error. Since, the proposed routing paths are not the shortest ones, additional transmission cost would be imposed on the network. It is shown in [22] that the data compression capability of sensor nodes and the routing strategy affect the transmission cost of the network. Since both schemes in [21,22] are based on sparse random measurements, they improve the energy consumption of WSNs. However, these methods suffer from the fact that the formation of routing trees in collecting of each CS measurement is not optimal, and this degrades the energy efficiency of WSNs. Reference [23] addresses this issue and proposes the Minimum Transmission data aggregation Tree (MTT) which forms a spanning tree based on the CS measurement matrix. Every node shares its sensed data for CS measurements only in a couple of times using the sparse random measurement matrix. The proposed algorithm in [23] forms the data aggregation tree based on the shortest path and the number of times that the nodes transmit their own data. Reference [24] proposes a tree-based energy efficient routing method to reduce the energy consumption of the WSN by considering the sensor transmission range and the probability of occurrence of non-zero elements in the measurement matrix. Following the same model as in [20], the authors in [25] introduce the Minimum Spanning Tree Projection (MSTP) which incorporates a compressive data aggregation method and the sparse random measurement to reduce the number of

141 transmissions and mitigates the energy consumption of
 142 whole network. Each projection node collects data of inter-
 143 est nodes and sends them to the sink node through a short-
 144 est path. The MSTP uses the Breath-First-Search (BFS) algo-
 145 rithm to form a spanning tree with the minimum number of
 146 transmission packets. The authors in [25] consider the “same
 147 transmission cost” for all sensor nodes and model the “un-
 148 weighted network graph”. In fact, regardless of energies re-
 149 quired to send data in different distances and without con-
 150 sidering the power control ability of sensor nodes, reference
 151 [25] assumes that all the nodes have the “same communica-
 152 tion ranges”.

153 Most of the works on the CS-based data aggregation con-
 154 sider tree-type routing methods in which a large number of
 155 sensor nodes take part in each CS measurement. It is shown
 156 in [26] that clustering is an efficient mechanism that sur-
 157 passes the tree-based routing methods in terms of the traf-
 158 fic load balancing and improves both energy consumption
 159 and the network’s lifetime. Reviewing the studies on the
 160 CS application in WSNs and to the best of our knowledge,
 161 there exists a few research works that investigate the CS
 162 theory for cluster-based WSNs [27,28]. In [27], the authors
 163 present centralized and distributed clustering algorithms for
 164 WSNs, in which cluster heads transmit data to the sink node
 165 through a backbone tree using a hybrid CS mechanism. How-
 166 ever, the work in [27] has ignored the fact that the sparse
 167 random measurement can be utilized in each cluster to de-
 168 crease the number of transmission packets. Reference [28]
 169 addresses this issue and presents a cluster-based data ag-
 170 gregation method with sparse random measurements in a
 171 star topology-based WSN. However, the star topology used
 172 in each cluster leads to an increase in the intra-cluster en-
 173 ergy consumption.

174 1.3. Contributions

175 Taking the above challenges into account, the key contri-
 176 butions of this work are summarized as follows:

- 177 • *Part I: Weighted Compressive Data Aggregation (WCDA)*
 178 *algorithm*: The main objective in the first part of this
 179 paper is to minimize the energy consumption of the
 180 network by utilizing the CDA and the sparse random
 181 measurement matrix (normally contains many zero
 182 elements) when compared with Non-CS and some
 183 classical CS-based data aggregation methods. To ad-
 184 dress this problem, a new algorithm, namely Weighted
 185 Compressive Data aggregation (WCDA), is proposed
 186 that aggregates the data from each node and effi-
 187 ciently sends them to the sink node. The novelty of our
 188 proposed WCDA algorithm lies in the power control
 189 ability in sensor nodes and weighted network graph
 190 which distinguish our work from the scheme in [25].
 191 In the proposed WCDA method, each transmit node
 192 adjusts its power level based on the Euclidean distance
 193 to the destination node to prevent more energy loss
 194 in the network. It is numerically shown that employ-
 195 ing the WCDA algorithm can significantly reduce the
 196 network’s energy consumption for the data transmis-
 197 sion between sensor nodes by forming efficient rout-
 198 ing trees and employing the load-balancing.

- 199 • *Part II: Cluster-based Weighted Compressive Data Ag-*
 200 *gregation (CWCDA)*: In the second part we modify the
 201 WCDA algorithm by jointly utilizing the CS-based data
 202 aggregation and the clustering to further reduce the
 203 energy consumption in the whole WSN. Note that the
 204 classical CS-based data aggregation methods such as
 205 plain-CS, hybrid-CS and the MSTP [25] are based on
 206 the tree routing which suffer from this fact that a
 207 large number of sensor nodes must be involved in
 208 each CS measurement. However, in the Cluster-based
 209 Weighted Compressive Data Aggregation (CWCDA)
 210 scheme, we apply the WCDA algorithm to each clus-
 211 ter in order to reduce significantly the number of in-
 212 volved sensor nodes during each CS measurement. In
 213 this case, candidate nodes related to each collector
 214 node are selected among the nodes inside one clus-
 215 ter. This yields in the formation of collection trees with
 216 a smaller structure than that of the WCDA algorithm.
 217 The effectiveness of these new algorithms is evaluated
 218 from the energy consumption, load balancing and life-
 219 time perspectives of the network. A comprehensive
 220 numerical evaluation is performed which shows that
 221 the performance of the proposed WCDA and CWCDA
 222 algorithms is significantly better than some existing
 223 data aggregation methods such as plain-CS, hybrid-CS
 224 and the Minimum Spanning Tree Projection (MSTP)
 225 schemes. Because the cluster-based data aggregation
 226 method generally has better traffic load balancing than
 227 the tree data aggregation method.

228 1.4. Paper organization

229 The rest of this paper is organized as follows. In [Section 2](#),
 230 the network model is described and the main assumptions
 231 and performance metrics required for our algorithms are in-
 232 troduced. [Section 3](#) introduces the basic concepts of CS the-
 233 ory and gives an overview of the CS-based data aggregation
 234 method in order to present the detail of the WCDA algorithm.
 235 [Section 4](#) deals with introducing the proposed CWCDA al-
 236 gorithm. [Section 5](#) reports our experiment and simulation
 237 results. Finally, in [Section 6](#), an overview of the results and
 238 some conclusion remarks are presented.

239 *Notations*: Throughout this paper, we use normal let-
 240 ters for scalars. Matrices and vectors are set in bold cap-
 241 ital and lower-case letters, respectively. $[.]^T$ indicates the
 242 transpose operator. In the vector domain, the concept of
 243 ℓ_p -norm is defined as $\|\mathbf{x}\|_p = (\sum_{i=1}^n |x_i|^p)^{1/p}$. \mathbb{R}^n means the
 244 n -dimensional real coordinate space. Finally, the ceiling no-
 245 tation $\lceil x \rceil$ is the smallest integer not less than x .

246 2. Model description and assumptions

247 2.1. Model description

248 In this work, we consider a multi-hop WSN consisting of
 249 n stationary and location-aware sensor nodes, denoted by
 250 $\{s_1, s_2, \dots, s_n\}$, which are distributed randomly throughout
 251 an $A \times A$ square area. The network contains the sink node de-
 252 noted by s_0 in a preassigned location that collects data from
 253 all sensor nodes. The system is modeled by a weighted bidi-
 254 rectional graph $G(\mathbf{V}, \mathbf{E})$ in which vertices set \mathbf{V} represents the

255 sink node and all the sensor nodes, and edge set \mathbf{E} represents
 256 bidirectional wireless links between nodes. For each link
 257 $i, j \in \mathbf{V}$, if a link exists, those nodes are in the communica-
 258 tion range of each other, or equivalently, a direct communica-
 259 tion between them is possible. We denote $w(i, j)$ as the *trans-*
 260 *mission cost* defined by the Euclidean distance between two
 261 nodes i, j . For each single-hop link $i, j \in \mathbf{V}$ with the Euclidean
 262 distance d_{ij} , the sensor node s_i transmits one data packet x_i
 263 of size L bits toward node s_j , where L is a fixed parameter
 264 for all the nodes. Assuming that all $s_i, i = 1, \dots, n$, have data
 265 packets for transmission at the beginning of each round, the
 266 main task of a data aggregation method is to aggregate ad-
 267 equate information for recovering the n -dimensional signal
 268 vector $\mathbf{x} = [x_1, \dots, x_n]^T$ at the sink node to minimize the en-
 269 ergy consumption of the network. In this paper, we assume
 270 that all interferences from different sources are controlled by
 271 the orthogonal signaling (e.g., Walsh–Hadamard codes [29])
 272 in the network. In addition, we suppose that no packet is lost
 273 during each transmission.

274 2.2. Performance metrics

275 To analyze and evaluate the performance of the underly-
 276 ing network, we use various performance metrics such as the
 277 energy consumption of each link, the load balancing, the First
 278 Node Dies (FND), and the tree's cost defined as follows.

279 • **Energy consumption:** We follow the same energy
 280 consumption model as in [30] for the link $i, j \in \mathbf{V}$ de-
 281 fined as

$$E_{T_i}(L, d) = E_{elec} \times L + \epsilon_{amp} \times L \times d_{ij}^2, \quad (1)$$

$$E_{R_j}(L) = E_{elec} \times L, \quad (2)$$

282 where $E_{T_i}(L, d)$ and $E_{R_j}(L)$ for all $i, j \in \mathbf{V}$ represent the
 283 energy consumption for sending and receiving one
 284 packet x_i of size L bits, for node i as the transmit-
 285 ter and node j as the receiver, respectively, E_{elec} rep-
 286 represents the consumed energy in receiving/sending of
 287 one-bit message via electrical circuits, and ϵ_{amp} de-
 288 notes the energy consumption of the transmission amp-
 289 lifier. It is assumed that each sensor node can ad-
 290 just its power level based on the distance from its
 291 corresponding destination. For such an energy model,
 292 we ignore the energy consumption of baseband sig-
 293 nal processing blocks such as source coding and pulse-
 294 shaping, as these energy consumptions are quite small
 295 compared to the energy consumption of the RF cir-
 296 cuitry [31].

298 • **Load balancing:** Let Γ_i represents the number of pack-
 299 ets transmitted by node s_i in each round. To quantify
 300 the performance of the load balancing of the proposed
 301 algorithms, we use the load variance metric denoted
 302 by S_n^2 for a given Γ_i of node s_i as follows:

$$S_n^2 = \frac{1}{n} \sum_{i=1}^n (\Gamma_i - \bar{\Gamma})^2, \quad (3)$$

303 where $\bar{\Gamma}$ denotes the average of the number of packets
 304 transmitted by node s_i in each round, obtained by

$$\bar{\Gamma} = \frac{1}{n} \sum_{i=1}^n \Gamma_i. \quad (4)$$

Clearly, lower S_n^2 leads to more traffic load balancing. 305

- **Network's lifetime:** The lifetime means the time du- 306
 ration that a network is operational and can perform 307
 its assigned tasks. In this work, we consider the First 308
 Node Dies (FND) as a performance metric to calculate 309
 the lifetime of the network which is defined as the 310
 number of rounds in which all nodes transmit their 311
 data to the sink node until the first node runs out of 312
 its energy. For such a definition, the main goal is to 313
 minimize the load variance of sensor nodes in order 314
 to maximize the network's lifetime. 315
- **Tree's cost:** The tree's cost is defined as the sum of the 316
 links' lengths of the tree. For instance, if a tree includes 317
 \mathcal{L} links and d_j denotes the length of j th link, then the 318
 tree's cost will be obtained as $\sum_{j=1}^{\mathcal{L}} d_j$. 319

3. Weighted Compressive Data Aggregation (WCDA) algorithm 320

321
 322 In this section, we propose a new data aggregation
 323 method, namely Weighted Compressive Data Aggregation
 324 (WCDA), for the network model introduced in Section 2. The
 325 main idea behind our proposed algorithm is to use both CS
 326 theory and sparse random measurements in the underlying
 327 weighted WSN graph in order to minimize the energy con-
 328 sumption and control the traffic load of the network. Before
 329 proceeding to the main part of this section, some primary
 330 concepts of CS theory and the sparse random measurements
 331 are briefly explained. We also discuss about the applications
 332 of CS theory in WSNs and describe in short some existing CS-
 333 based data aggregation methods for the upcoming fair com-
 334 parison. 334

3.1. Compressive sampling theory 335

336 Compressive sampling theory is a promising methodol-
 337 ogy in digital signal processing for reconstructing sparse sig-
 338 nals with very few measurements under a certain basis [10].
 339 Indeed, CS theory offers a possibility of high resolution cap-
 340 ture of compressible signals from relatively few data mea-
 341 surements, typically below the number of data obtained from
 342 the optimal Shannon/Nyquist sampling theorem. CS theory
 343 declares that signal vector $\mathbf{x} = [x_1, \dots, x_n]^T$ is k -sparse, if it
 344 has at most k non-zero coefficients in which x_i 's represent
 345 the signal samples and n denotes the signal's dimension.
 346 Typically, signals in some WSN applications are not sparse,
 347 but they have a sparse representation $\mathbf{x} = \Psi\alpha$ on the basis
 348 of compression $\Psi_{n \times n} = [\psi_1, \dots, \psi_n]$ with column vectors ψ_i
 349 where $\alpha = [\alpha_1, \dots, \alpha_n]^T$ is the sparse equivalent of the origi-
 350 nal signal \mathbf{x} . CS theory states that if signal \mathbf{x} on basis of Ψ has
 351 a k -sparse representation so that $\mathbf{x} = \sum_{i=1}^k \alpha_i \psi_i$ and $k \ll n$,
 352 under certain conditions and using $\mathbf{y} = [y_1, \dots, y_m]^T = \Phi\mathbf{x}$,
 353 the original signal can be recovered from just $m = \mathcal{O}(k \log n)$
 354 samples instead of collecting all samples of signal \mathbf{x} [10]. For
 355 $m \times n$ measurement matrix $\Phi = [\phi_1, \dots, \phi_n]$, the row vec-
 356 tors ϕ_i should have large incoherent with the compression
 357 basis Ψ , or the Restricted Isometry Property (RIP) for the
 358 measurement matrix $\Theta_{m \times n} = \Phi_{m \times n} \Psi_{n \times n}$ is established. It
 359 is shown in [11] that measurement matrix Φ satisfies the RIP of
 360 order $2k$ if $\delta_k \in (0, 1)$ so that the following statement is true

361 for the signal \mathbf{x} with a k -sparse representation:

$$(1 - \delta_k) \|\mathbf{x}\|_2^2 \leq \|\Phi \mathbf{x}\|_2^2 \leq (1 + \delta_k) \|\mathbf{x}\|_2^2. \quad (5)$$

362 Existence of the RIP for random matrices such as Gaus-
363 sian matrix with uniformly and independently distributed
364 elements and Bernoulli matrix with ± 1 elements has been
365 proved in [11]. The reconstruction process is equivalent
366 to finding the signal's sparse coefficient vector α , which
367 can be cast into an ℓ_1 -norm convex optimization problem
368 that recovers the signal \mathbf{x} using the CS measurements $\mathbf{y} =$
369 $[y_1, \dots, y_m]^T$ [12]:

$$\min_{\alpha \in \mathbb{R}^n} \|\alpha\|_{\ell_1} \quad \text{subject to} \quad \mathbf{y} = \Phi \Psi \alpha = \Theta \alpha. \quad (6)$$

370 It is worth mentioning that the practical performance of
371 the CS theory depends on the amount of the signal sparse-
372 ness and the recovery algorithms. Also, in this theory, in-
373 creasing the number of CS measurements will enhance the
374 quality of the data recovery [10].

375 3.2. Application of compressive sampling in WSNs

376 The ultimate goal of our WSN model is that each node
377 s_i transmits its measured data x_i to the sink node s_0 such
378 that a vector $\mathbf{x} = [x_1, \dots, x_n]^T$ is formed at s_0 . In the Non-
379 Compressive Sampling (Non-CS) data aggregation method,
380 shown in Fig. 1a, each child s_i , $i \in \{1, \dots, v-1\}$, sends a sam-
381 ple to v th node, so that the output link of this node sends
382 v packets to its parent through a preassigned path. Clearly
383 for the Non-CS method, the nodes near to the sink node suffer
384 from the heavy data traffic and lose their energies quickly
385 leading to the network's lifetime degradation. One heuristic
386 solution to alleviate this bottleneck problem is to apply the
387 CS theory in the above data aggregation process. The main
388 idea behind this CS-based data aggregation is illustrated in
389 Fig. 1b, where at the beginning of each round, the node s_i , $i \in$
390 $1, \dots, n$, extends its data to an m -dimensional vector $\mathbf{u}_i = x_i \phi_i$
391 with $m \ll n$, and sends the extended vector to its parent.
392 For this method, suppose that m is predefined and known in
393 the whole network, and each node s_i is aware of its own m -
394 dimensional coding vector ϕ_i . Then, each parent node adds
395 its extended data to that of its children, and this procedure
396 is repeated until all the aggregated data arrive at the sink
397 node s_0 . Eventually, the sink node collects all CS measure-
398 ments $y_i = \sum_{j=1}^n x_j \phi_{ij}$, $i = 1, \dots, m$, and then the recovery
399 algorithm is used to reconstruct the n raw samples.

400 Applying the principles of CS theory directly on the data
401 aggregation process, namely Plain-CS shown in Fig. 1a, every
402 node requires to send m packets to its parent, thus, the traf-
403 fic load on each link will always be the same and it equals to
404 m . Therefore, the sink node receives an m -dimensional vec-
405 tor instead of n -dimensional vector as in the Non-CS method.
406 Then, the sink node recovers x_i , $i = 1, \dots, n$, by a preassigned
407 recovery algorithm. The above Plain CS-based data aggrega-
408 tion method benefits from the fact that the decoding process
409 in each node is carried out in a distributed manner by some
410 simple and low computational cost operations such as addi-
411 tion and multiplication. In fact, the main computational load
412 is pushed to the decoding phase on the sink node s_0 which
413 is limitless in terms of the energy consumption. In the Plain-
414 CS method, the total number of data packet transmissions for
415 data collection from all nodes is equal to mn . It is evident that

with an increase in m , the number of transmitted packets in-
efficiently increases. In addition, the Plain-CS method leads
to an unnecessary increase in the traffic load in early stages
of the transmission. As a result, applying CS theory naively on
each node may not be the best choice in the Plain-CS method.

In another data aggregation method, namely the Hybrid-
CS algorithm proposed in [17], if the number of transmission
packets is larger than CS measurements, i.e., $v > m$ the links
between the nodes carry out dense random measurements,
otherwise, as long as the number of output samples is less
than m , the sensor employs the Non-CS method which only
relays data packets (see Fig. 1a). It is shown in [17] that the
Hybrid-CS method outperforms both Non-CS and Plain-CS
schemes in terms of the energy efficiency.

One challenge faced in the aforementioned data aggrega-
tion methods is that they have utilized the dense random
measurement matrix, while they have missed the fact that
matrix Φ may contain many zero entries. On the other hand,
in the data aggregation using sparse random measurements,
the measurement matrix includes many zero elements. In
the sparse case, each sensor node participates in the CS mea-
surement only if its respective ϕ_{ij} is non-zero, while for the
aforementioned Plain-CS and Hybrid-CS methods with dense
random measurements, all sensors involve in CS measure-
ments. It is shown in [20] that the transmission cost per
sample measurement is reduced from $\mathcal{O}(n)$ for dense ran-
dom measurements to $\mathcal{O}(\log n)$ for sparse random measure-
ments. The authors in [20] state that there is a compromise
between the number of non-zero elements in each row of
measurement matrix Φ and the number of rows it contains.
However, the problem in [20] is that a minimum tree's cost
for overall network cannot be guaranteed, because for each
random measurement, a large number of transmissions is
required to collect data at the measurement node without
any proper path. Another challenge for the aforementioned
schemes is that they suffer from the lack of power control
ability in sensor nodes and use energy inefficient routing al-
gorithms in the network.

3.3. Proposed WCDA algorithm

According to the challenges discussed in section 3.2,
we propose an efficient data aggregation method, namely
Weighted Compressive Data Aggregation (WCDA) algorithm,
which benefits from the advantages of sparse random mea-
surements and the power control ability in sensor nodes.
The proposed WCDA algorithm forms energy efficient rout-
ing trees with focus on the load-balancing issue to improve
both lifetime and energy efficiency of the network.

Let start by briefly describing the features of the sparse
random measurement matrix Φ introduced in [20] which
normally contains many zero elements. The measurement
matrix Φ must satisfy two following conditions:

(1) In order to distribute non-zero elements uniformly in
each row of measurement matrix Φ with dimension $m \times n$
and maximize its sparseness, the number of non-zero ele-
ments in each row of Φ must be as $\kappa = \lceil n/m \rceil$.

(2) It is necessary to have no column with all zero ele-
ments in measurement matrix Φ , because each column of
matrix Φ corresponds to a sensor node. Thus, if a column
of matrix Φ has full zero elements, then the data from its

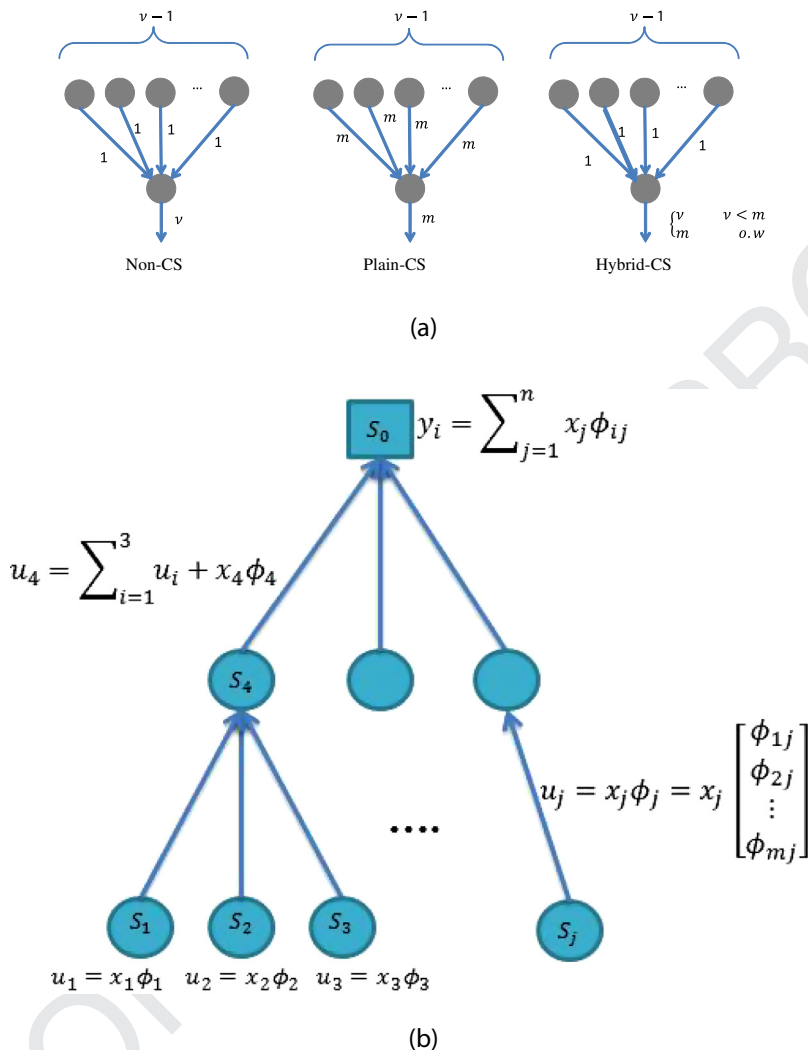


Fig. 1. (a) Comparison of three data aggregation methods in multi-hop WSNs. The link labels represent the number of transmission packets on each link during one data aggregation round, and (b) A typical structure of the CS-based data aggregation method in multi-hop WSNs.

475 corresponding sensor node is discarded. Each sensor node
 476 $s_i, i = 1, \dots, n$, needs to store a column of measurement matrix
 477 Φ , denoted by vector ϕ_i , in its memory.

478 To satisfy the above conditions, the distribution process of
 479 elements in each row of measurement matrix Φ is performed
 480 as follows (see the typical matrix Φ with dimension 4×12
 481 in (7) as well):

$$\Phi = \begin{bmatrix} \phi_{1,1} & 0 & 0 & 0 & 0 & \phi_{1,6} & 0 & 0 & 0 & \phi_{1,10} & 0 & 0 \\ 0 & 0 & 0 & \phi_{2,4} & \phi_{2,5} & 0 & \phi_{2,7} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \phi_{3,8} & \phi_{3,9} & 0 & \phi_{3,11} & 0 \\ 0 & \phi_{4,2} & \phi_{4,3} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \phi_{4,12} \end{bmatrix} \quad (7)$$

- 482 • **Step 1:** Uniformly distribute $\kappa = \lceil n/m \rceil$ non-zero elements
 483 in the first row, while the remaining $n - \kappa$ entries are considered zero.
- 484 • **Step 2:** Uniformly distribute κ non-zero elements
 485 among the remaining $n - \kappa$ entries in the i^{th} row, $i =$
 486 $1, \dots, m$, in which the remaining entries in the i^{th} row
 487 are those have considered zero in all previous rows.
- 488 • **Step 3:** $i + 1 \leftarrow i$
- 489 • **Step 4:** Repeat step 2 till all m rows of measurement
 490 matrix Φ are filled.
 491

Recall that each node s_i measures one sample x_i which
 492 has a spatial correlation with its adjacent nodes. According to
 493 the CS theory, the sink node s_0 requires only m random
 494 CS measurement $y_i = \sum_{j=1}^n x_j \phi_{ij}, i = 1, \dots, m$, to recover all
 495 samples of the sensor nodes. For this purpose, m nodes are
 496 chosen uniformly as *collector nodes*, denoted by $\{r_1, r_2, \dots,$
 497 $r_m\}$, to collect CS measurements in the network. Each collector
 498 node r_i aims to collect one random CS measurement y_i
 499 and transmits y_i to the sink node. Toward this goal, the i
 500 row of measurement matrix Φ , denoted by ϕ_{r_i} , is allocated
 501 to $r_i, i = 1, \dots, m$. For the i th collector node, the correspond-
 502 ing nodes with $\phi_{ij} \neq 0$ (in the i th row of Φ) are defined as the
 503

504 candidate nodes $a_k, k = 1, \dots, \kappa$. We denote $\mathcal{T}_i, i = 1, \dots, m$,
505 as the collection tree corresponding to collector node r_i as its
506 root. This tree is spread using the proposed WCDA algorithm
507 until all the candidate nodes are included.

508 The pseudo-code of our WCDA algorithm is outlined in
509 Algorithm 1. The network graph $G(\mathbf{V}, \mathbf{E})$, the collector nodes
510 and the sparse random measurement matrix Φ act as the in-
511 puts of the WCDA algorithm. In each round of performing the
512 WCDA algorithm, one heuristic matrix belonging to the col-
513 lection tree \mathcal{T}_i with three rows is created, in which the first,
514 second and third rows indicate the tree nodes, the parent of
515 each node and the Euclidean distance between each node
516 and its parent, respectively. The procedure of the proposed
517 WCDA algorithm is perform as follows:

- 518 • **Step 1: Initialization:** The candidate nodes correspond-
519 ing to collector node r_i , represented with the set
520 Int_i , are placed in the set $intTmp$. To form \mathcal{T}_i , the collec-
521 tor node r_i with the zero tree's cost is considered as the
522 only node without parent. If r_i is one of the candidate
523 node, it is removed from the set $intTmp$.
- 524 • **Step 2: Single-hop candidate node:** The collection
525 tree is extended by adding the candidate nodes which
526 can be connected to the current tree with a single-
527 hop. This process is carried out during the *While* loop
528 in the lines 5–18 of Algorithm 1. The candidate node
529 is connected to the current tree via the link by which
530 the tree's cost is minimized. The parent of the candi-
531 date node a_i is defined as the node that connects a_i to
532 the current tree. Then, the nodes connected to the tree
533 with the only single-hop connection are removed from
534 the set $intTmp$. Thus, the set $intTmp$ shows the remain-
535 ing candidate nodes which are still not connected to
536 the tree. If this set is empty, the failure criteria of the
537 infinite loop in the line 4 has been met and there is no
538 need to run the rest of the algorithm; otherwise, go to
539 Step 3.
- 540 • **Step 3: Multi-hop candidate node:** Among the re-
541 maining candidate nodes located in a multi-hop con-
542 nection of the current tree, the nearest one will be con-
543 nected to the tree via the shortest path. This process
544 is run by two nested loops in lines 23 and 24 of the
545 pseudo-code. Since the network graph is weighted, we
546 use the *dijkstra* algorithm [32] to find the shortest path
547 \mathcal{P} from the candidate node in a multi-hop route to the
548 current tree. All existing nodes in the path \mathcal{P} is added
549 to the tree by the *for* loop in the line 29 of Algorithm 1.
550 Then, the candidate node connected to the tree by a
551 multi-hop route is removed from the set $intTmp$.
- 552 • **Step 4: Data aggregation:** The above steps are re-
553 peated until all the single-hop and multi-hop candi-
554 date nodes are connected to the tree. After forming
555 the collection tree \mathcal{T}_i and noting that each node s_j
556 in \mathcal{T}_i knows its parent and children nodes, compute
557 $u_j = x_j \phi_{ij}$. Then, according to the CS-based data aggre-
558 gation, each node s_j aggregates u_j with its children's
559 data and sends the aggregated data packet to its par-
560 ent node. Once the collector node r_i receives the ran-
561 dom CS measurement $y_i = \sum_{j=1}^n x_j \phi_{ij}$, it sends y_i to
562 the sink node in the form of a data packet through
563 the shortest path between the collector nodes and the

564 sink node. The WCDA algorithm is performed for all
565 collector nodes so that collection tree $\mathcal{T}_i, i = 1, \dots, m$,
566 for each collector node r_i is formed. Similarly, other
567 collector nodes aggregate their measured samples and
568 send them to the sink node. Finally, m collection trees
569 are formed in the network, each constitutes one of the
570 random CS measurements y_i . In this step, the proposed
571 WCDA algorithm uses the *dijkstra* algorithm [32] to
572 find a possible shortest path.

Algorithm 1 WCDA.

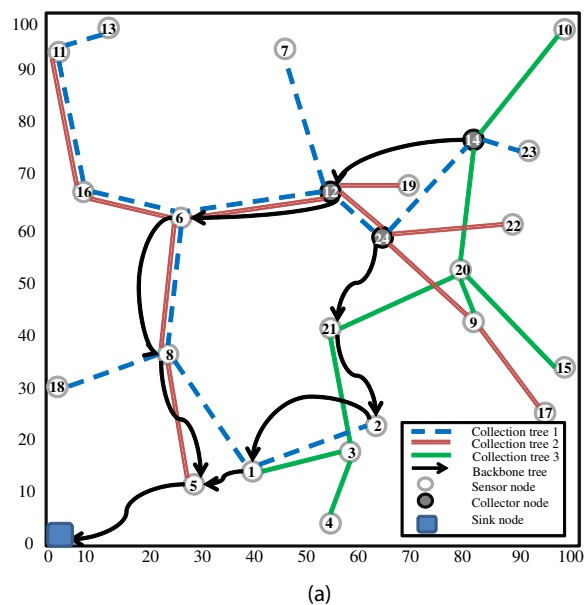
Inputs: $G(\mathbf{V}, \mathbf{E}), \{r_1, r_2, \dots, r_m\}, \Phi$
Outputs: $\mathcal{T}_i, i = 1, \dots, m$

```

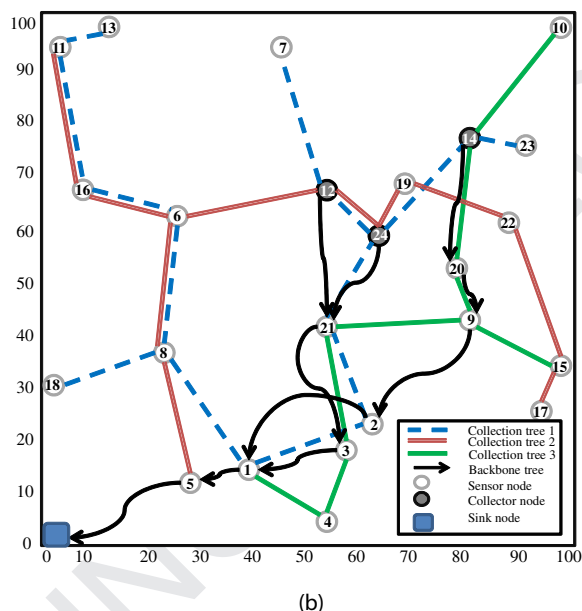
1: for  $i = 1$  to  $m$  do
2:    $intTmp \leftarrow Int_i$ 
3:    $tree \leftarrow [p_i - 1 \ 0]^T$ 
4:   While ( $intTmp$  is not empty)
5:     Do
6:       for  $C = 1$  to  $N_{intTmp}$  do
7:         for  $k = 1$  to  $N_{Tree}$  do
8:           if  $adj(intTmp(C), tree(1,k))$  then
9:              $dist \leftarrow [distance(intTmp(C), tree(1, k))$ 
10:               $tree(1, k)]^T$ 
11:           end if
12:         end for
13:       if  $N_{dist} > 0$  then
14:          $m \leftarrow find\ min(dist)$ 
15:          $tree \leftarrow [intTmp(C) \ dist(2, m) \ dist(1, m)]^T$ 
16:          $remove(intTmp, C)$ 
17:       end if
18:     end for
19:   While ( $N_{dist} > 0$ )
20:   if  $N_{intTmp} = 0$  then
21:     Break while
22:   end if
23:    $Cst \leftarrow \infty; \mathcal{P} \leftarrow [];$ 
24:   for  $l = 1$  to  $N_{intTmp}$  do
25:     for  $k = 1$  to  $N_{Tree}$  do
26:        $Cst \leftarrow \min(Cst, Cost(dijkstra\ shortest\ path$ 
27:         $(tree(1, k), intTmp(l)))$ 
28:        $\mathcal{P} \leftarrow path(min_{Cst})$ 
29:     end for
30:   end for
31:   for all Nodes  $n$  in path  $\mathcal{P}$  do
32:      $tree \leftarrow [n \ pred(n) \ distance(n, pred(n))]^T$ 
33:   end for
34:    $remove(intTmp, min_{Cst})$ 
35:   end While
36:    $CollectionTree(i) \leftarrow tree$ 
37: end for
38: return  $CollectionTree(i), Cst$ 

```

572 To get more insight into the described WCDA algorithm
573 and to compare that with the MSTP algorithm [25], let con-
574 sider a network with 24 sensor nodes shown in Fig 2. In this
575 network, nodes 12, 14 and 24 are uniformly selected as the
576 collector nodes. According to the sparse random measure-
577 ment matrix Φ with dimension 3×24 , the candidate nodes
578 of the first collector node (i.e., root 24) are the nodes 12, 13,
579



(a)



(b)

Fig. 2. A typical WSN with $n = 24$ and $m = 3$. (a) MSTP algorithm, and (b) Proposed WCDA algorithm.

8, 14, 7 and 23. In both WCDA and MSTP algorithms, the first collection tree \mathcal{T}_1 considers the node 24 as its root and is spread until all the candidate nodes are included. The nodes 12 and 14 are the single-hop candidate nodes of \mathcal{T}_1 , which are directly connected to node 24 in the first step of both algorithms. The next candidate nodes in both algorithms are 23 and 7 which must be connected to the current tree via a node having the shortest path. Accordingly, node 23 to node 14 and node 7 to node 12 are connected. In the next step, one of two multi-hop collector nodes 2 or 8 should be added to the current tree. Since, the MSTP algorithm is performed based on the number of hops, it does not discriminate

between nodes 8 and 2, thus, it connects the node 8 to the current tree via the Breath-First-Search (BFS) algorithm [33]. In this case, an efficient path cannot be selected based on the energy consumption. However in our WCDA algorithm, the node 2 is connected to the current tree earlier than the node 8, as node 2 has a smaller Euclidean distance with the current tree than node 8. This selected shortest path results in a higher energy efficiency than the corresponded path node 8 as will be shown in Section 5. After forming the collection trees \mathcal{T}_1 , \mathcal{T}_2 and \mathcal{T}_3 , the collector nodes 12, 14 and 24 aggregate the data of their candidate nodes based on the CS-based data aggregation process and send them to the sink node through the shortest path. This backbone tree is shown with the directional lines (\rightarrow) in Fig 2. As seen in this figure, the proposed WCDA algorithm aims to select the efficient paths to minimize the energy consumptions in (1) and (2). Numerical results show that the energy consumptions in the WCDA and MSTP algorithms are 0.0611 and 0.0994 Jules, respectively. We see that our proposed WCDA algorithm displays 38.53% more energy efficient than the MSTP algorithm which suffers from the lack of a power control ability. Our WCDA algorithm benefits from this advantage that one specific node does not need to set its power level at the maximum, once it sends data to its nearest node and adjusts its power based on the Euclidean distance. This leads to more efficiently improvement in the formation process of the collection trees than the MSTP scheme.

4. Cluster-based Weighted Compressive Data Aggregation (CWCDA)

The existing CS-based data aggregation methods (e.g., Plain-CS, Hybrid-CS, MSTP) rely on routing trees, in which a large number of sensor nodes are deployed in each CS measurement. Thus, these methods consume more energy which yields they are not practically feasible in WSNs. On the other hand, since candidate nodes in the WCDA algorithm are uniformly selected, some of them may be far from each other. For such a situation and to create each CS measurement y_i , $i = 1, \dots, m$, a collection tree with lots of links is formed which increases the tree's cost. The above challenges motivate us to propose an energy efficient method, namely Cluster-based Weighted Compressive Data Aggregation (CWCDA), to make a significant reduction in the energy consumption in our WSN model. The main idea behind this algorithm is to apply the WCDA algorithm to each cluster in order to reduce significantly the number of involved sensor nodes during each CS measurement. In this case, candidate nodes related to each collector node are selected among the nodes inside one cluster. This yields in the formation of collection trees with a smaller structure than that of the WCDA algorithm.

In the proposed CWCDA algorithm, we divide the WSN into n_c local non-overlapping clusters, denoted by $C = \{c_1, \dots, c_{n_c}\}$, using the simple and well-known K-means algorithm [34], in which the sink node separately aggregates the data of all clusters. For this algorithm, when the clustering process is performed uniformly, the number of sensors in each cluster for a large value of n is approximated by n/n_c . The maximum communication range of each node in cluster c_k , denoted by R_{c_k} , is obtained when the graph is continuous

651 in each cluster. Before describing the CWCD algorithm,
652 we go through the properties of the Block Diagonal Matrix
653 (BDM) which is formed based on the cluster-based data
654 aggregation.

655 4.1. Block diagonal matrix (BDM)

656 The block diagonal matrix presented in this paper is a ma-
657 trix with a total of n_C sub-matrices Φ_k , $k = 1, \dots, n_C$, each
658 Φ_k has the individual size $m_k \times n_k$, whereas other nondi-
659 agonal entries of the BDM are all zero. Suppose the signal
660 $\mathbf{x} \in \mathbb{R}^n$ is partitioned into n_C vectors $\mathbf{x}_k \in \mathbb{R}^{n_k}$ and for each
661 $k \in \{1, \dots, n_C\}$, sub-matrix $\Phi_k: \mathbb{R}^{n_k} \rightarrow \mathbb{R}^{m_k}$ collects the CS
662 measurements $\mathbf{y}_k = \Phi_k \mathbf{x}_k$. The total CS measurement vector
663 $\mathbf{y} = [\mathbf{y}_1^T, \dots, \mathbf{y}_{n_C}^T]^T \in \mathbb{R}^m$ is given by

$$\mathbf{y} = \Phi \mathbf{x} \Leftrightarrow \begin{bmatrix} \mathbf{y}_1 \\ \mathbf{y}_2 \\ \vdots \\ \mathbf{y}_{n_C} \end{bmatrix} = \begin{bmatrix} \Phi_1 & 0 & \dots & 0 \\ 0 & \Phi_2 & \ddots & \vdots \\ \vdots & \ddots & \ddots & 0 \\ 0 & \dots & 0 & \Phi_{n_C} \end{bmatrix} \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \\ \vdots \\ \mathbf{x}_{n_C} \end{bmatrix}. \quad (8)$$

664 In this paper, we suppose that Φ_k is a sparse random mea-
665 surement matrix which is formed according to the proce-
666 dure explained in Section 3.3. It is shown in [35] that the
667 BDM Φ satisfies the RIP condition and it can be considered
668 as an effective measurement matrix. Reference [35] demon-
669 strates that the random sampling BDM can be used for the
670 signal recovery by the CS theory. The number of CS mea-
671 surements m depends on the compression basis Ψ in which the
672 signal is sparse. If the measurement matrix has a low coher-
673 ence with the compression basis (e.g., Fourier basis or DCT
674 basis), increasing n_C results in a more sparse measurement
675 matrix, while n_C does not increase with m . In other words, if
676 the measurement matrix has a high coherence with the com-
677 pression basis, m would be considered as a linear function of
678 n_C . With respect to the structure of this measurement matrix,
679 the BDM Φ can be converted to a sparse random measure-
680 ment matrix after permutation of their rows and columns
681 [35]. Thus, a BDM with sparse random measurements blocks
682 can also satisfy the RIP condition.

683 In the proposed CWCD algorithm, the measurement ma-
684 trix created in the sink node is not in the shape of the tradi-
685 tional dense random measurement matrix with the Gaussian
686 or Rademacher elements. In fact, the CS-based data aggre-
687 gation method creates a BDM consisting of several sampling
688 sub-matrices Φ_k , $k = 1, \dots, n_C$, each Φ_k belongs to the k th
689 cluster. We denote n_k and m_k as the number of nodes and
690 the CS measurements for k th cluster, respectively. Since, m_k
691 is a linear function of the number of nodes n_k in cluster c_k ,
692 it concludes that $m_k = (n_k/n) \times m$, $k = 1, \dots, n_C$. Similar to
693 the WCDA algorithm described in Section 3.3, in the CWCD
694 scheme, the sink node aggregates $m = \sum_{k=1}^{n_C} m_k$ CS mea-
695 surements \mathbf{y}_i , $i = 1, \dots, n$, however, the traffic load in each cluster
696 c_k is reduced to m_k CS measurements.

4.2. Proposed CWCD algorithm

The CWCD scheme has been described in details in
Algorithm 2. The network graph $G(\mathbf{V}, \mathbf{E})$, the number of clus-

Algorithm 2 The proposed CWCD algorithm.

Inputs : $G(\mathbf{V}, \mathbf{E})$, n_C , E_p
Outputs : $\mathcal{T}_{i,k}$, $i = 1, \dots, m_k$, \mathcal{T}_k , $k = 1, \dots, n_C$, \mathcal{B}_T

- 1: Divide nodes into n_C clusters using K-means algorithm.
- 2: **while** all $E_i > 0$, $i = 1, \dots, n$ **do**
- 3: **for** each cluster c_k , $k = 1, \dots, n_C$ **do**
- 4: **if** first round **then**
- 5: Assign nearest cluster node to center of the cluster as cluster head
- 6: **else**
- 7: Assign cluster node with the most remaining energy as cluster head
- 8: **end if**
- 9: Find R_{c_k} for a continuous graph of each cluster
- 10: Create $Distance_{c_k}$ and $Adjacent_{c_k}$ relative to $Range_{c_k}$
- 11: Distribute m_k collector nodes among clusters corresponding to number of their nodes
- 12: Assign $\lceil n_k/m_k \rceil$ candidate nodes for each collector node in cluster c_k
- 13: Build collection Trees $\mathcal{T}_{i,k}$ in each cluster using Algorithm 1
- 14: **for** each collector node r_i **do**
- 15: Find the shortest path from r_i to corresponding cluster head
- 16: **end for**
- 17: **end for**
- 18: **for** each cluster head c_k , $k = 1, \dots, n_C$ **do**
- 19: Find shortest path to s_0
- 20: **end for**
- 21: **for** all nodes **do**
- 22: calculate consumed E_i
- 23: **end for**
- 24: **end while**

699 ters n_C , and the primary energy of the node, denoted by E_p
700 (identical for all the nodes), are the inputs of this algorithm.
701 We denote E_i , $i = 1, \dots, n$, as the residual energy of each
702 node. The outputs of the CWCD algorithm are as follows:
703

- **Collection tree:** We denote $\mathcal{T}_{i,k}$, $i = 1, \dots, m_k$, as the
collection tree corresponding to the i th collector node
in cluster c_k . This tree is spread using the WCDA algo-
rithm introduced in Section 3.3 until all the candidate
nodes in cluster c_k are included.
- **Cluster head tree:** The cluster head tree, denoted
by \mathcal{T}_k , $k = 1, \dots, n_C$, corresponding to the k th cluster
head, includes the cluster head as its root and all col-
lector nodes.
- **Backbone tree:** The backbone tree, denoted by \mathcal{B}_T , con-
sists of the sink node (considered as its root) which
connects all cluster heads to the sink node.

To get more insight into how this algorithm works, we
consider the scenario shown in Fig. 3 to describe the pro-
posed CWCD algorithm as follows:

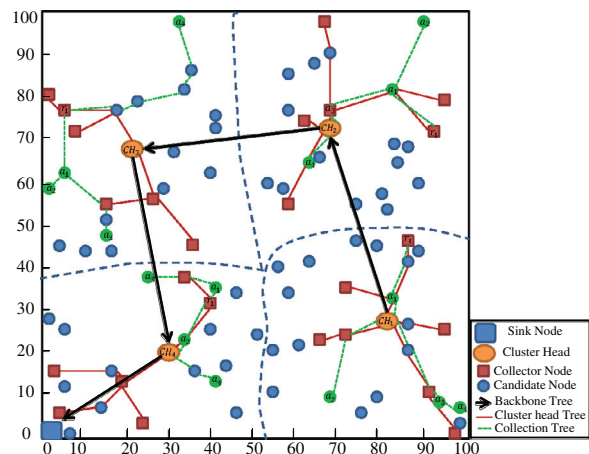


Fig. 3. A typical structure of the CWCD algorithm in a multi-hop WSN.

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- **Step 1: Initialization:** We divide all sensor nodes in the network into n_c clusters using K-means algorithm [34]. In each cluster c_k , $m_k = (n_k/n) \times m$, $k = 1, \dots, n_c$, collector nodes are chosen randomly. We consider $\lceil n_k/m_k \rceil$ candidate nodes for each collector node in cluster c_k .
- **Step 2: Cluster Head election:** It is a well known fact that the cluster head election affects on the energy consumption in each clustering method [36]. For this purpose, in the first round of the CWCD algorithm (as shown in Fig. 3), the midpoint of each cluster is identified, and then the nearest node to the selected midpoint is chosen as the Cluster Head (CH). This type of CH's election minimizes the intra-cluster energy consumption. In the next rounds, the node with a more residual energy is selected as the CH that balances the energy consumption over the whole network. In this case, the energy consumption is minimum within each cluster.
- **Step 3: Intra-cluster data aggregation:** This step employs the WCDA algorithm to form the collection trees for each cluster, in which data of candidate nodes are aggregated by collector nodes. Fig. 3 only presents one collection tree $\mathcal{T}_{1,k}$, shown with dash lines, for the first collector node r_1 in cluster c_k . Then, the collector nodes in each cluster c_k send their data to the corresponding CH using the shortest path tree, namely cluster head tree \mathcal{T}_k , $k = 1, \dots, n_c$. To find the shortest path, the *dijkstra* algorithm [32] is used.
- **Step 4: Inter-cluster data aggregation:** In each round, the k th CH aggregates its own m_k received CS measurements y_k and then, all data of CHs are sent to the sink node through a backbone tree. To form the backbone tree as a shortest path tree between CHs, the proposed CWCD algorithm makes a graph $\mathbf{G}_{ch} = (\mathbf{V}_{ch}, \mathbf{E}_{ch})$ in which \mathbf{V}_{ch} is a set of the sink node and the CHs, while \mathbf{E}_{ch} denotes the links between these nodes. In the graph formation, the algorithm calculates the maximum communication range, R_{min} , for a graph that contains the CHs and the sink node so that our graph is finally continuous. In each round, the k th CH collects m_k measured samples of its sensor nodes and

forms $y_i = \sum_{j=1}^{n_k} \phi_{ij} x_j$, $i = 1, \dots, m_k$. Then, the vector $\mathbf{x} = [\mathbf{x}_1^T, \mathbf{x}_2^T, \dots, \mathbf{x}_{n_c}^T]^T$ of size $n = n_1 + n_2 + \dots + n_{n_c}$ is formed where $\mathbf{x}_k \in \mathbb{R}^{n_k}$ denotes the data of n_k sensor nodes in k th cluster. When the sink node receives all $m \ll n$ CS measurements from the CHs, it can recover the original data of all sensor nodes. Finally, the CWCD algorithm calculates the residual energy for all the nodes to choose the node with the highest residual energy as the CH in the next round.

- **Step 5: Terminate:** The algorithm is terminated when at least one E_i , $i = 1, \dots, n$, is equal to zero.

5. Simulation results

In this section, we evaluate and compare the performances of the proposed WCDA and CWCD algorithms in different scenarios with the existing conventional data aggregation methods such as Non-CS, Hybrid-CS [17] and MSTP [25] in a weighted WSN in terms of the energy consumption, the load balancing and the network's lifetime. For the scenarios under simulation, we investigate the effect of (i) location variation of the sink node, (ii) the number of CS measurements, and (iii) the number of sensor nodes, on the aforementioned performance metrics, and show the superiority of our algorithms compared with traditional data aggregation methods.

5.1. Simulation setup

We consider a WSN in which the nodes are randomly distributed with the uniform distribution inside a square area with the size $100 \times 100 m^2$. It is assumed that there exists a spatial correlation between the sensed data of sensor nodes. To apply this correlation on our simulations, we suppose that data of all sensor nodes have a sparse representation based on the Discrete Cosine Transform (DCT) basis. All simulations have been run in the MATLAB software. In our simulations, only the energy consumption of sending and receiving data over the network is computed, and we ignore the energy consumed by the data routing information. This assumption is used in many relevant literature (e.g., [25,28]). In addition, we set $E_{elec} = 50 nJ/bit$, $\epsilon_{amp} = 100 pJ/bit/m^2$ and the length of data packets is $L = 1024$ bits [30]. The primary energy of all nodes is set to $E_p = 2J$. In addition, we compute the average of each performance metric over 10 runs of one algorithm with different measurement matrix Φ and different collector nodes. We consider the *normalized reconstruction error* defined as $\frac{\|\mathbf{x} - \hat{\mathbf{x}}\|_2}{\|\mathbf{x}\|_2}$ in the CS signal recovery stage in which the vectors \mathbf{x} and $\hat{\mathbf{x}}$ represent the original and the recovered signals, respectively. We evaluate the accuracy of our proposed methods using the real-world data collected by the LUCE WSN deployment at the EPFL [37] which focuses on the ambient temperature values.

5.2. Evaluation and comparison

First scenario: In this scenario, we set $n = 1000$ and $m = 100$ for the algorithms under simulation, and the number of clusters $n_c = 10$ for the CWCD scheme. The validation of selection $n_c = 10$ will be provided numerically at the end of this section. In addition, the position of the sink node will

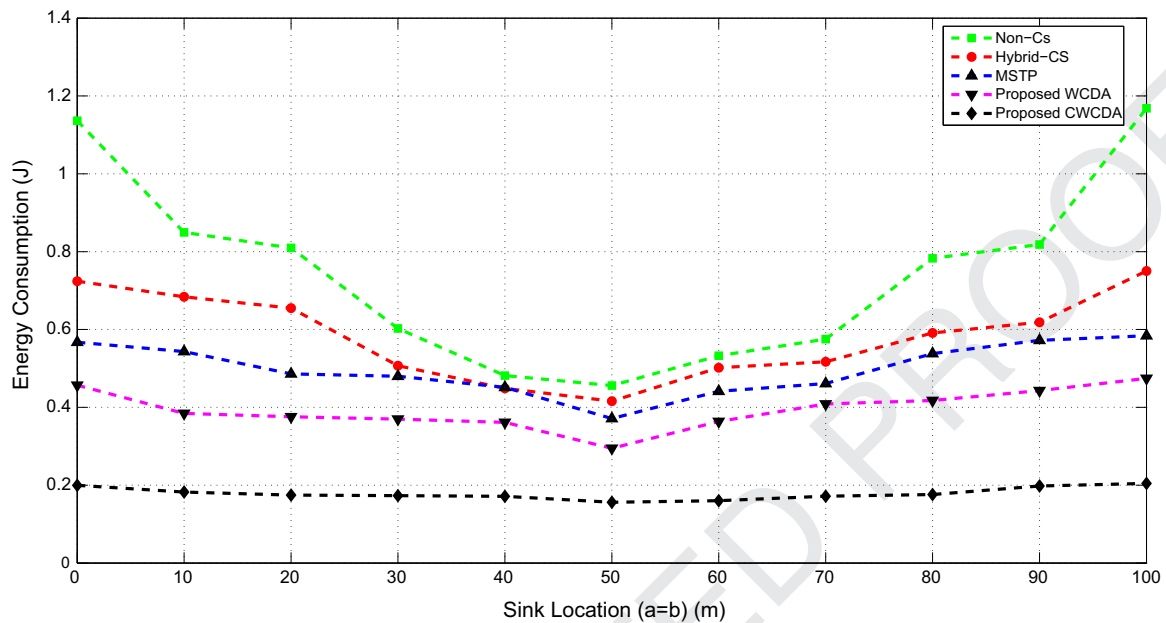


Fig. 4. Comparison of the energy consumption in Non-CS, Hybrid-CS, MSTP, WCDA and CWCDa data aggregation methods for $n = 1000$ when the sink node location varies on the main diameter ($a = b$).

Table 1

Comparison of load variance in Non-CS, Hybrid-CS, MSTP, WCDA and CWCDa data aggregation methods for $n = 1000$ when the sink node location varies on the main diameter ($a = b$ meter).

| Algorithm | $a = 0$ | $a = 10$ | $a = 20$ | $a = 30$ | $a = 40$ | $a = 50$ | $a = 60$ | $a = 70$ | $a = 80$ | $a = 90$ | $a = 100$ |
|----------------|---------|----------|----------|----------|----------|--------------|----------|----------|----------|----------|-----------|
| Non-CS | 4612.8 | 2494.6 | 2105.8 | 837.4 | 722.2 | 613.5 | 766.1 | 1174.1 | 1497.4 | 2919.2 | 4210.9 |
| Hybrid-CS | 663.6 | 592.7 | 569.2 | 443.2 | 425.3 | 399.7 | 418.7 | 464.7 | 549.0 | 647.5 | 727.3 |
| MSTP | 91.7 | 77.8 | 68.3 | 53.7 | 51.4 | 48.4 | 46.6 | 57.6 | 60.8 | 74.6 | 86.7 |
| Proposed WCDA | 75.1 | 66.0 | 64.6 | 49.4 | 46.8 | 43.5 | 43.5 | 57.3 | 59.8 | 73.1 | 81.1 |
| Proposed CWCDa | 38.5 | 30.7 | 19.9 | 17.9 | 15.4 | 13.0 | 13.3 | 16.1 | 18.2 | 36.8 | 47.8 |

816 be changed on the main diameter of the square area of the
 817 network to find the best place for this node in terms of the
 818 energy consumption. Fig. 4 compares the energy consumption
 819 of the proposed WCDA and CWCDa schemes with that of
 820 the traditional Non-CS, Hybrid-CS [17] and MSTP [25] meth-
 821 ods versus the sink node location. Note that the natural vari-
 822 ables $a, b \in [0, 100]$ represent the geographic coordinates of
 823 the sink node location on the main diameter, i.e., $a = b$ in
 824 Fig. 4. It is observed from Fig. 4 that the energy consump-
 825 tion of all traditional data aggregation methods, in particular
 826 the Non-CS scheme, strongly depends on the location of the
 827 sink node. In fact, the best position for the sink node to min-
 828 imize the energy consumption in all schemes is the center
 829 of the network area. The main reason for this better perfor-
 830 mance is that the tree which connects the sensor nodes to
 831 the sink node is shortest in this point. The interesting result
 832 extracted from Fig. 4 is that the energy consumption of the
 833 proposed CWCDa scheme is almost robust against the loca-
 834 tion of the sink node. Furthermore, our algorithms exhibit a
 835 lower energy consumption in each location of the sink node
 836 when compared to other data aggregation methods. This can
 837 be justified for noting that in our WCDA algorithm, one spe-
 838 cific sensor node does not need to adjust its power on the
 839 maximum value once it sends data to its nearest node. In fact,

840 each sensor node sets its power level based on the Euclidean
 841 distance to the destination node. In addition, in the CWCDa
 842 algorithm, candidate nodes related to each collector node are
 843 selected among the nodes within one cluster. Therefore, the
 844 number of participated sensor nodes during each CS measure-
 845 ment is reduced. This leads to a more energy efficiency than
 846 other schemes.

847 Table 1 provides a fair comparison for the load variance
 848 S_n^2 defined in (3) for the aforementioned data aggregation
 849 algorithms in different sink node locations $a = b$. As seen
 850 from Table 1, for all data aggregation methods, the minimum
 851 S_n^2 is achieved when the sink node is located at the center
 852 of the network area, because the number of nodes in the
 853 neighborhood of the centered sink node is maximum. The
 854 results in Table 1 demonstrate that the WCDA, CWCDa and
 855 MSTP outperform the conventional Non-CS and Hybrid-CS
 856 methods from the load variance points of view. The worst
 857 case for load balancing belongs to the Non-CS method. In fact
 858 for the Non-CS scheme, the number of transmission packets
 859 in each round for the sensors is different, as the sensors near
 860 to the sink node send more packets than leaf nodes. This
 861 leads to a more energy consumption for the nodes in the
 862 vicinity of the sink node. In contrast, our CWCDa algorithm
 863 outperforms significantly the other schemes in terms of load

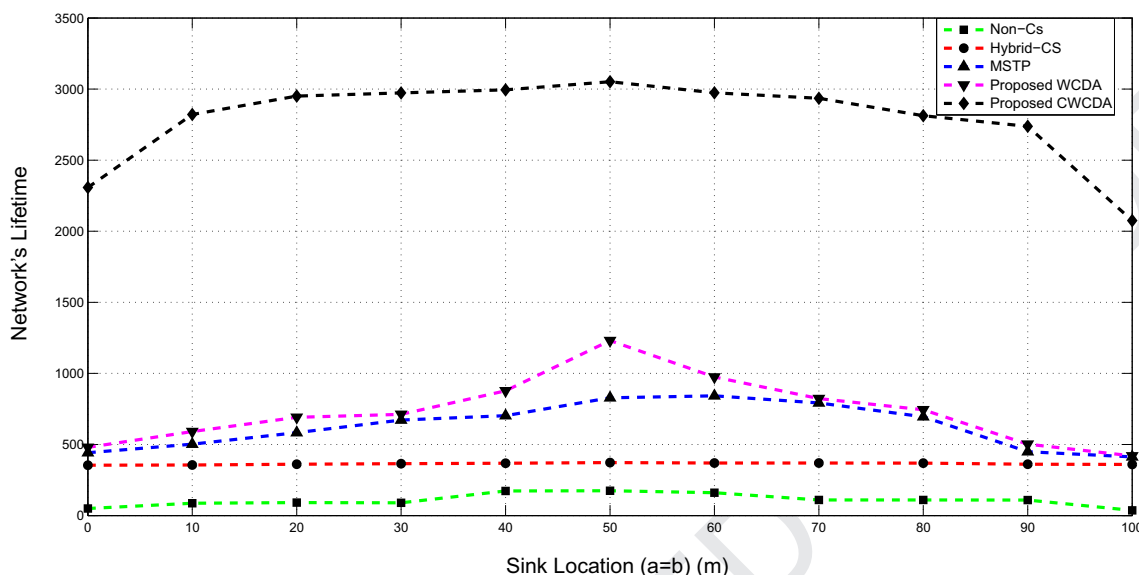


Fig. 5. Comparison of the network's lifetime in Non-CS, Hybrid-CS, MSTP, WCDA and CWCDA data aggregation methods for $n = 1000$ when the sink node location varies on the main diameter ($a = b$).

864 balancing. This superior performance comes from the fact
 865 that the distance of leaf nodes to the root of the collection
 866 tree is too short, thus, the collection tree corresponding
 867 to each collector node within a cluster experiences more
 868 enhanced balancing in the collection tree comparing to the
 869 case when the clustering method is not utilized.

870 To complete the evaluation of the first scenario, we compare
 871 in Fig. 5 the network's lifetime of the aforementioned
 872 algorithms in different sink node locations when the first
 873 node dies. As illustrated in Fig. 5, the maximum lifetime of
 874 the network for all data aggregation methods is obtained
 875 when the sink node is located again in the center of the
 876 network's area. This result comes exactly from the results in
 877 Fig. 4 and Table 1, where the energy consumption and the
 878 load variance are in the minimum values at this point. Similarly,
 879 the proposed WCDA and CWCDA schemes outperform the
 880 conventional Non-CS, Hybrid-CS and MSTP methods in
 881 terms of the network's lifetime. The interesting result from
 882 Fig. 5 is that the network's lifetime in the proposed CWCDA
 883 is significantly better than the proposed WCDA, due to the
 884 following reasons:

885 (i) Totally, the network's lifetime of cluster-based algorithms
 886 is more than that of non clustering methods [26].

887 (ii) In the CWCDA scheme, less sensor nodes are involved
 888 in the collection tree formation.

889 (iii) Of course, it should be noted that in a typical cluster-
 890 based algorithm, cluster heads consume more energy than
 891 other nodes that leads to a reduction in the lifetime of the
 892 network. However, we employ a heuristic cluster head election
 893 in the CWCDA scheme described in Section 4.2 to overcome
 894 the above problem in enhancing the network's lifetime.

895 **Second scenario:** In this scenario, we evaluate the effect
 896 of the number of CS measurements, $m \in [10, 250]$, on the
 897 network's performance, where we consider again a WSN with
 898 $n = 1000$ sensor nodes and the number of clusters, $n_c = 10$,
 899 for the CWCDA algorithm. We assume that the sink node

900 is located at coordinate (0, 0). We follow the same performance
 901 metrics as in the first scenario to compare our proposed
 902 WCDA and CWCDA schemes with that of the conventional
 903 Non-CS, Hybrid-CS and MSTP methods. According to the
 904 results in Fig. 6, the minimum energy consumption of the
 905 networks in all schemes is achieved when parameter m is set
 906 at the minimum value, i.e., $m = 10$. This leads to a reduction
 907 in the number of collection trees and the number of packets
 908 transmitted to the sink node. On the other hand, as shown in
 909 Table 2 and based on CS theory, we know that reducing the CS
 910 measurement m increases the reconstruction error of signals
 911 in the network. Thus, there exists a compromise between the
 912 energy consumption and the data reconstruction error when
 913 m changes. With a similar arguments as in the first scenario,
 914 the best scheme in terms of the minimum energy consumption
 915 is the CWCDA algorithm for different values of m .

916 As seen from Table 3, an increase in the number of CS
 917 measurements m leads to an increase in the difference of the
 918 loads between the leaf nodes and the sensors around the sink
 919 node, hence, the load variance of all CS-based data aggregation
 920 methods will be increased. Accordingly, as well as the reasons
 921 mentioned in the first scenario, the WCDA, CWCDA
 922 and MSTP outperform the conventional Non-CS and Hybrid-
 923 CS schemes in terms of the load balancing for each value of
 924 m . On the other hand, for all data aggregation methods, by
 925 increasing the number of CS measurements, the lifetime of the
 926 network is reduced, because the number of collection trees
 927 and the number of packets transmitted by each node will be
 928 increased, as observed in Fig. 7.

929 **Third scenario:** In the last scenario, we evaluate the
 930 effect of changing the number of sensor nodes n on the
 931 performance of the proposed WCDA and CWCDA methods and
 932 compare their energy consumptions, load balancing and the
 933 network's lifetime with the aforementioned classical data
 934 aggregation methods. In this scenario, the sink node is located
 935 at coordinate (0, 0). For all values of n , the number of CS

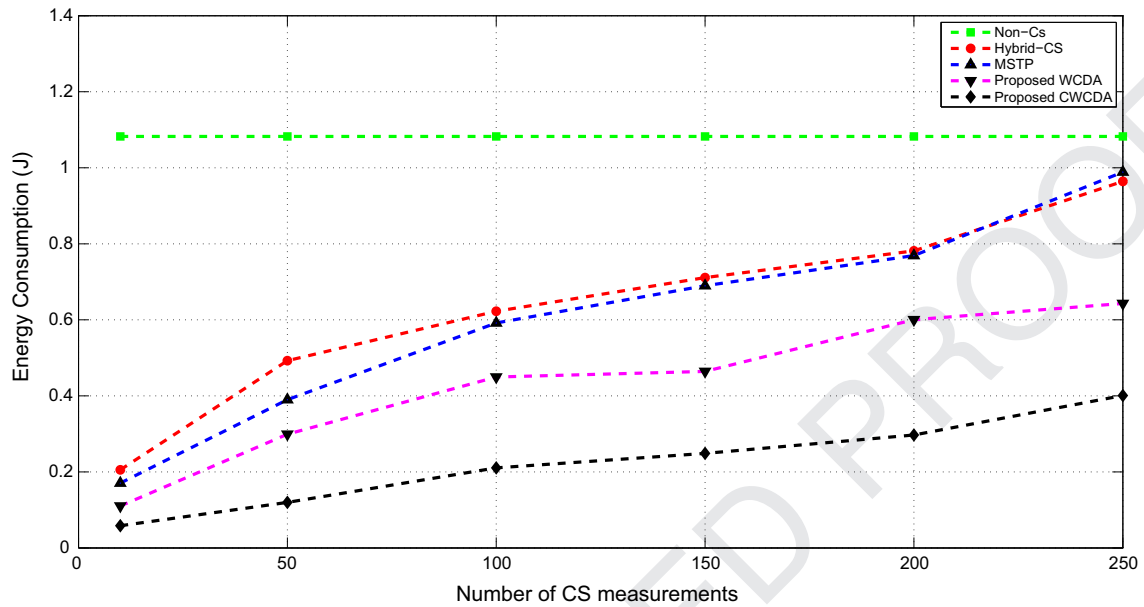


Fig. 6. Comparison of the energy consumption in Non-CS, Hybrid-CS, MSTP, WCDa and CWCDa data aggregation methods for $n = 1000$ with changing the number of CS measurements in the range [10,250].

Table 2

Comparison of data reconstruction error in WCDa and CWCDa methods for $n = 1000$ and different values of the number of CS measurements.

| Data aggregation method | $m = 10$ | $m = 50$ | $m = 100$ | $m = 150$ | $m = 200$ | $m = 250$ |
|-------------------------|----------|----------|-----------|-----------|-----------|-----------|
| Proposed WCDa | 0.29075 | 0.14145 | 0.06246 | 0.04766 | 0.04468 | 0.04216 |
| Proposed CWCDa | 0.29220 | 0.08815 | 0.07959 | 0.04851 | 0.04695 | 0.04415 |

Table 3

Comparison of load variance in Non-CS, Hybrid-CS, MSTP, WCDa and CWCDa data aggregation methods for $n = 1000$ and different values of the number of CS measurements.

| Data aggregation method | $m = 10$ | $m = 50$ | $m = 100$ | $m = 150$ | $m = 200$ | $m = 250$ |
|-------------------------|----------|----------|-----------|-----------|-----------|-----------|
| Non-CS | 3673 | 3673 | 3673 | 3673 | 3673 | 3673 |
| Hybrid-CS | 13.9 | 240.8 | 619.0 | 918.2 | 1456.1 | 1916.2 |
| MSTP | 1.8 | 32.5 | 91.2 | 220.5 | 317.4 | 454.6 |
| Proposed WCDa | 1.7 | 22.1 | 90.6 | 109.9 | 298.2 | 370.7 |
| Proposed CWCDa | 0.2 | 10.3 | 50.3 | 78.9 | 131.1 | 229.8 |

measurements is set to $m = n/10$. As previously mentioned, in the CWCDa algorithm, the total number of CS measurements increases linearly with the number of clusters n_c , therefore, we consider $n_c = m/10$. It is clearly predictable that with an increase in the number of sensor nodes n , the number of packets transmitted over the network is increased and as a result, the energy consumption and the load variance grow, however, the lifetime of the network will be reduced, as respectively observed from Fig. 8, Table 4 and Fig. 9. With the same arguments as in previous scenarios, our CWCDa scheme outperforms significantly other classical data aggregation methods in particular from the energy efficiency points of view.

Remark 1: In the final step of our simulation, we check the validation of selecting the number of cluster $n_c = 10$ in all previous simulations. Toward this goal, we run the proposed CWCDa scheme with different values of n_c , and set $n = 1000$ and $m = 100$, in order to evaluate the effect of n_c on

the energy consumption as shown in Fig. 10. It is seen from Fig. 10 that the total energy consumption of the networks is a monotonically decreasing function of n_c , meaning that more clusters in the network results in more energy saving. However, it is shown in [35] that an increase in the number of clusters leads to an increase in the reconstruction error. Thus, we have a tradeoff between the energy consumption and the reconstruction error in terms of n_c . Since the reduction rate of the energy consumption in Fig. 10 is sufficiently low for $n_c \geq 10$, we set $n_c = 10$ in all simulations for the CWCDa scheme to guarantee an acceptable reconstruction error in our system model.

Remark 2: To complete our simulation results, we consider the following physical layer channel model and the practical energy efficiency in the physical layer which is widely utilized in many WSN literature (e.g., please see references [2,4,38]). Toward this goal, we consider the uncoded M-ary FSK modulation where M orthogonal carriers can be

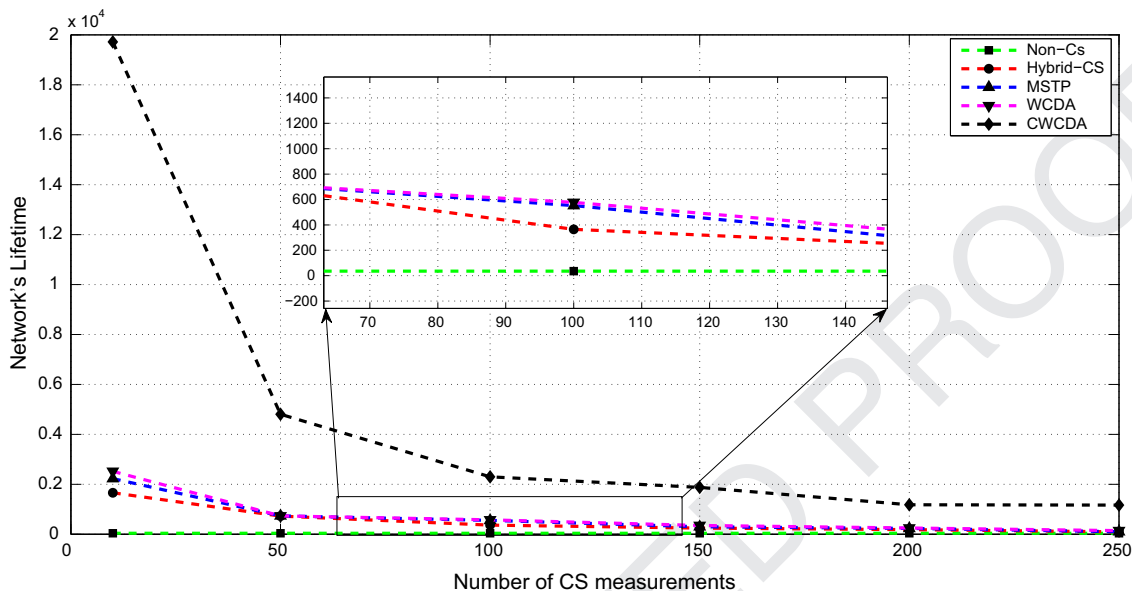


Fig. 7. Comparison of lifetime in Non-CS, Hybrid-CS, MSTP, WCDA and CWCDA data aggregation methods for $n = 1000$ with changing the number of CS measurements in the range [10,250]

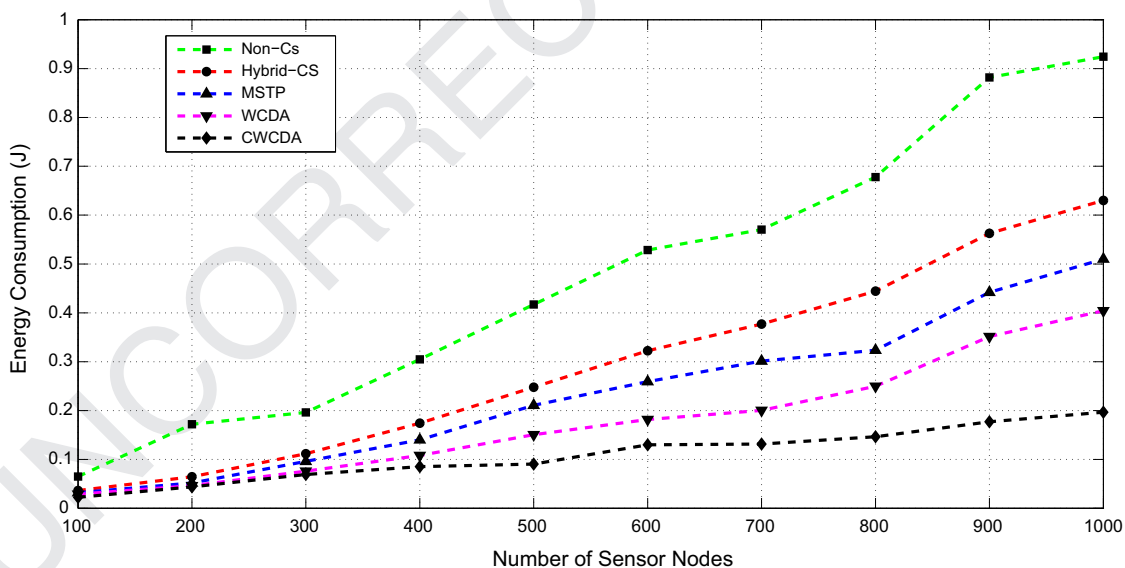


Fig. 8. Comparison of the energy consumption in Non-CS, Hybrid-CS, MSTP, WCDA and CWCDA data aggregation methods with changing the number of sensor node $n \in [100, 1000]$.

Table 4

Comparison of load variance in Non-CS, Hybrid-CS, MSTP, WCDA and CWCDA data aggregation methods with changing the number of sensor node.

| Data aggregation method | n = 100 | n = 200 | n = 300 | n = 400 | n = 500 | n = 600 | n = 700 | n = 800 | n = 900 | n = 1000 |
|-------------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|
| Non-CS | 239.3 | 331.6 | 392.2 | 640.0 | 768.3 | 1412.8 | 1885.7 | 2127.7 | 3293.2 | 4131.3 |
| Hybrid-CS | 13.1 | 30.1 | 68.8 | 139.1 | 173.4 | 290.6 | 383.5 | 476.2 | 524.7 | 597.2 |
| MSTP | 12.8 | 25.3 | 32.0 | 37.8 | 49.8 | 68.5 | 70.3 | 79.2 | 89.6 | 98.2 |
| Proposed WCDA | 12.8 | 14.9 | 22.5 | 26.1 | 35.5 | 48.0 | 58.9 | 59.0 | 65.9 | 74.7 |
| Proposed CWCDA | 7.3 | 11.9 | 13.5 | 18.8 | 26.6 | 28.5 | 29.3 | 33.7 | 36.1 | 41.9 |

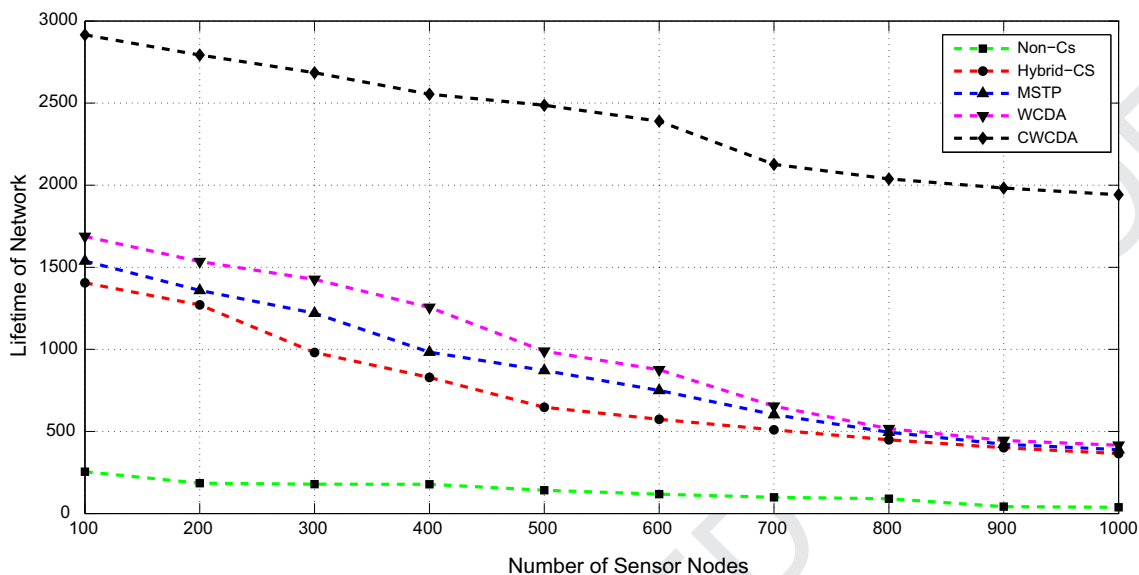


Fig. 9. Comparison of the network's lifetime in Non-CS, Hybrid-CS, MSTP, WCDA and CWCDA data aggregation methods with changing the number of sensor node $n \in [100, 1000]$.

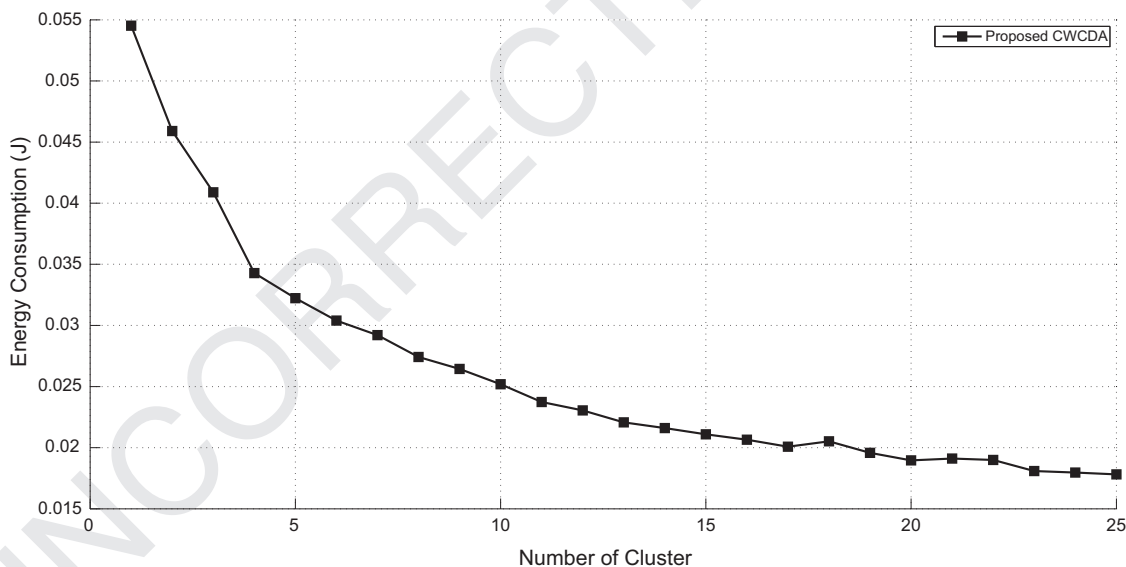


Fig. 10. Comparison of energy consumption in CWCDA algorithm with changing the number of cluster n_c .

972 mapped into $b \triangleq \log_2 M$ bits. It is shown in [39] that the transmit
 973 energy consumption per each symbol for an uncoded
 974 MFSK with non-coherent detector is obtained as

$$\mathcal{E}_t \triangleq \left[(1 - (1 - P_s)^{\frac{1}{M-1}})^{-1} - 2 \right] \frac{\mathcal{L}_d N_0}{\Omega} \quad (9)$$

975

$$\stackrel{(a)}{=} \left[\left(1 - \left(1 - \frac{2(M-1)}{M} P_b \right)^{\frac{1}{M-1}} \right)^{-1} - 2 \right] \frac{\mathcal{L}_d N_0}{\Omega}, \quad (10)$$

976 where (a) comes from the fact that the relationship between
 977 the average Symbol Error Rate (SER) P_s and the average Bit
 978 Error Rate (BER) P_b of MFSK is given by $P_s = \frac{2(M-1)}{M} P_b$. For
 979 the above equations and for a η th power path-loss channel,

980 the channel gain factor is given by $\mathcal{L}_d = M_l d^\eta \mathcal{L}_1$, where M_l
 981 is the gain margin which accounts for the effects of hard-
 982 ware process variations, background noise and $\mathcal{L}_1 \triangleq \frac{(4\pi)^2}{G_t G_r \lambda^2}$
 983 is the gain factor at $d = 1$ meter which is specified by the
 984 transmitter and receiver antenna gains G_t and G_r , and wave-
 985 length λ . In addition, we denote the fading channel coeffi-
 986 cient corresponding to symbol i as h_i , where the amplitude
 987 $|h_i|$ is Rayleigh distributed with probability density function
 988 (pdf) $f_{|h_i|}(r) = \frac{2r}{\Omega} e^{-\frac{r^2}{\Omega}}, r \geq 0$, where $\Omega \triangleq \mathbb{E}[|h_i|^2]$.

989 According to introduced physical layer channel model, the
 990 effect of the number of CS measurements, $m \in [10, 250]$, on
 991 the network's performance is evaluated and the results are

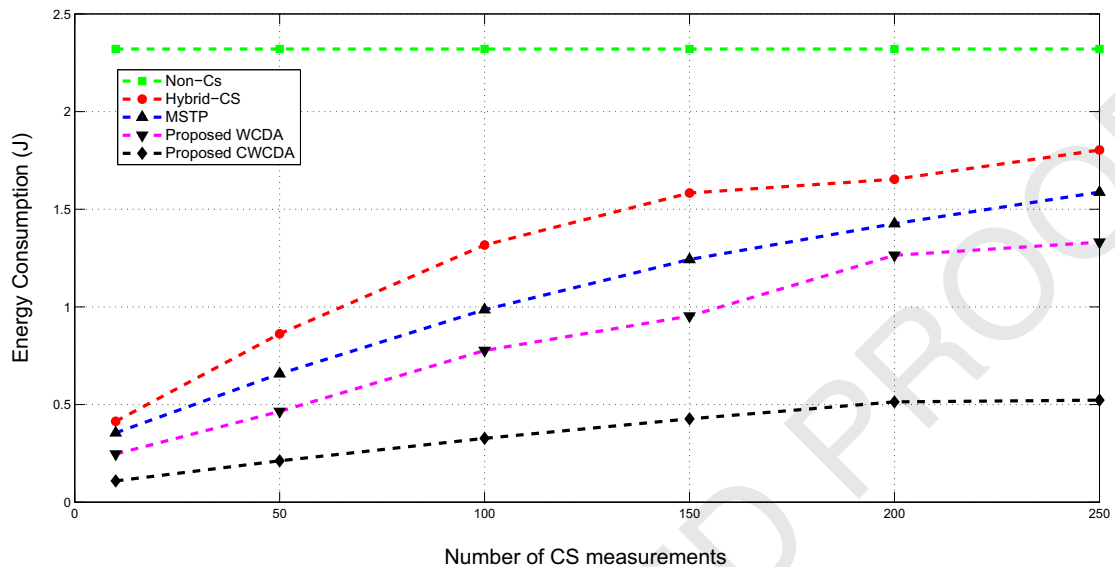


Fig. 11. Comparison of the energy consumption in Non-CS, Hybrid-CS, MSTP, WCDA and CWCA data aggregation methods for $n = 1000$ with changing the number of CS measurements in the range $[10,250]$ with taking the physical layer channel model into account.

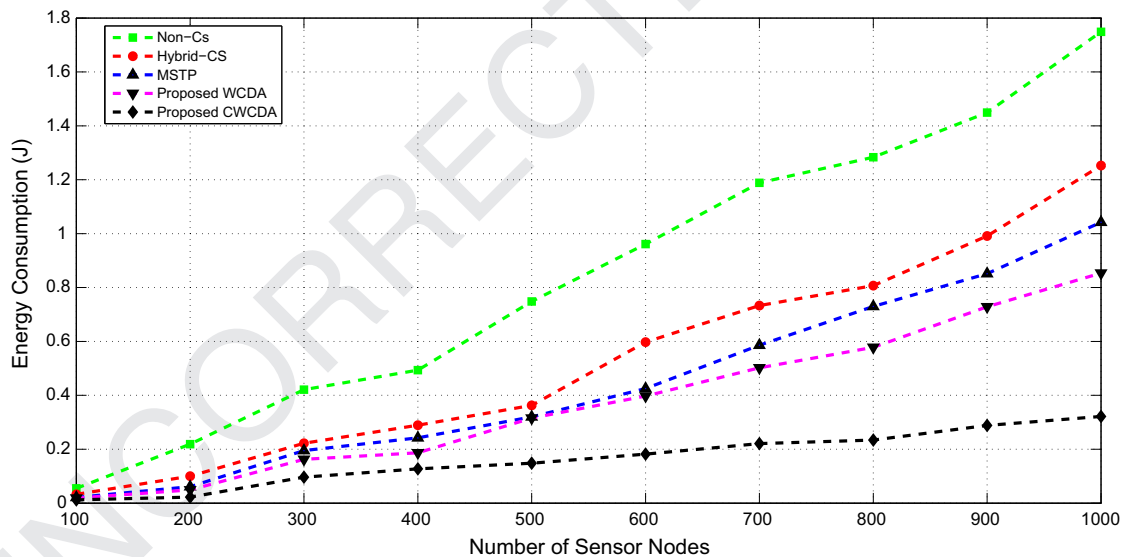


Fig. 12. Comparison of the energy consumption in Non-CS, Hybrid-CS, MSTP, WCDA and CWCA data aggregation methods with changing the number of sensor nodes $n \in [100, 1000]$ with taking the physical layer channel model into account.

992 demonstrated in Fig. 11, where we consider again a WSN with
 993 $n = 1000$ sensor nodes and the number of clusters, $n_C = 10$,
 994 for the CWCA algorithm. Like to previous scenarios, we assume
 995 that the sink node is located at coordinate $(0, 0)$. Then,
 996 the proposed WCDA and CWCA schemes are compared with
 997 the conventional Non-CS, Hybrid-CS and MSTP methods. As it
 998 can be seen from Fig. 11, with taking the physical layer
 999 channel model into account in the second scenario, the proposed
 1000 schemes yet have the best performance in terms of the energy
 1001 consumption for different values of m .

1002 By considering the specifications and assumptions presented
 1003 in third scenario and using the aforementioned physical layer
 1004 channel model, the simulations have been repeated

and the results have been shown in Fig. 12. As observed
 1005 from Fig. 12, the proposed methods, especially CWCA, have
 1006 lower energy consumption with compared to the conventional
 1007 schemes.
 1008

6. Conclusion

1009
 1010 In this paper, we used the compressive sampling and
 1011 the power control ability in sensor nodes to propose a new
 1012 energy efficient data aggregation scheme in a weighted WSN
 1013 model, called “Weighted Compressive Data Aggregation
 1014 (WCDA)”. It was demonstrated that the proposed WCDA
 1015 algorithm uniformly selects collector nodes to form the

collection tree in which each collector node aggregates a CS measurement from the corresponding candidate nodes, and then, each collector node sends the CS measurements to the sink node. We also extended the WCDA scheme to a new algorithm, namely “Cluster-based Weighted Compressive Data Aggregation (CWCD)”, to reduce more energy consumption based on an integration of the clustering method and the compressive sampling. Our work has focused on the improvement of the energy consumption, load balancing and the network’s lifetime in different scenarios and has compared our proposed methods with three conventional schemes, Non-CS, Hybrid-CS and MSTP, which has demonstrated a superior efficiency of our proposed schemes. In particular, we derived numerical results for the aforementioned performance metrics in terms of the sink node locations, the number of CS measurements, and the number of sensor nodes. Numerical results have shown 20% energy saving for the WCDA algorithm keeping at the same time 10% lower load variance when compared to the MSTP algorithm in [25] when the sink node is located at the center of network’s area. For this sensor node’s location, the CWCD algorithm performs 47% better than the WCDA scheme in terms of the energy consumption. In another scenario, when the number of CS measurements is 10 times the number of sensor nodes in the network, our simulation results showed that the WCDA scheme can reduce the energy consumption by about 24% when compared with the MSTP method. Meanwhile, the CWCD algorithm can reduce the energy consumption up to 53% compared to the WCDA method. Overall, the CWCD algorithm is attractive for using in large-scale WSNs already has the advantages of less energy consumption and load variance than classical CS-based data aggregation methods. However, the proposed CWCD algorithm sacrifices 21% more data reconstruction error than the classical MSTP and WCDA schemes.

In this paper, we have selected randomly collector nodes in all proposed algorithms. A possible future extension of this work would be to find the optimal positions of collector nodes which minimize the energy consumption. In addition, this paper has focused on the spatial correlation properties of sensed data in real WSNs. A particularly nice extension of this work is to take into account both spatial and temporal correlations between sensors data in the proposed algorithms.

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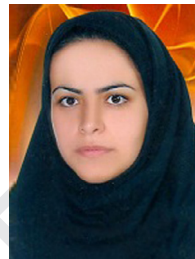
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